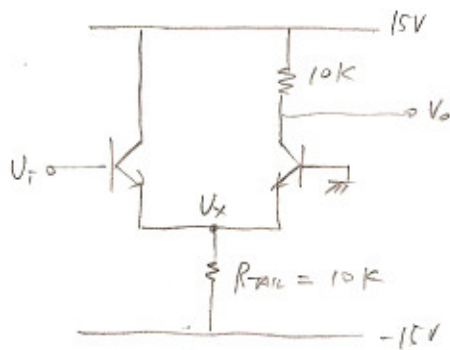


3.20



R_{in}
 A_v
 R_{out}

$$I_{C1} = I_{C2} = \frac{1}{2} \cdot \frac{15 - 0.7}{10K} = 0.71 \text{ mA} \quad \text{assume } V_{be} = 0.7 \text{ V}$$

$$g_{m1} = g_{m2} = \frac{0.71 \text{ mA}}{26 \text{ mV}} = 27.3 \text{ mA/V}$$

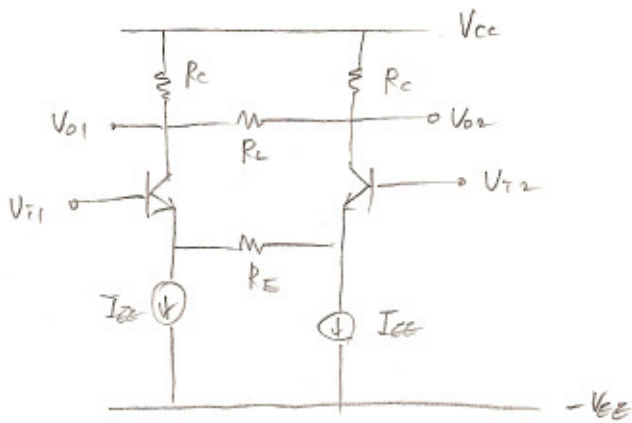
$$r_{\pi 1} = r_{\pi 2} = \frac{\beta}{g_m} = \frac{200}{27.3 \text{ mA/V}} = 7.33 \text{ k}\Omega$$

$$R_{in} = r_{\pi 1} + (1 + \beta) \left(\frac{1}{g_{m2}} \parallel R_{tail} \right) \approx 2r_{\pi} = 14.6 \text{ k}\Omega$$

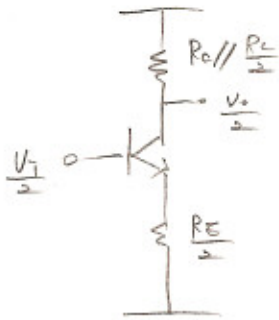
$$A_v = \frac{V_x}{V_i} \cdot \frac{V_o}{V_x} \approx \frac{1}{2} \cdot g_{m2} \cdot R_C = 136.5$$

$$R_o = R_C = 10 \text{ k}\Omega$$

3.21



↓ half circuit (DM)



$$R_{in, dm} = 2 \left\{ r_{\pi} + (\beta + 1) \frac{R_E}{2} \right\}$$

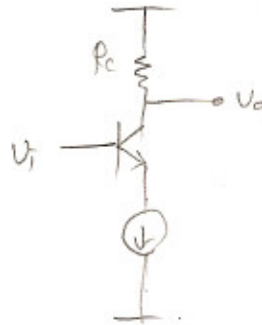
$$= 2r_{\pi} + (\beta + 1) R_E$$

$$A_{dm} = \frac{g_m (R_c // \frac{R_c}{2})}{1 + g_m \frac{R_E}{2} (\beta + 1)}$$

$$= \frac{r_{\pi} g_m (R_c // \frac{R_c}{2})}{r_{\pi} + (\beta + 1) \frac{R_E}{2}}$$

A_{cm}
 A_{dm}
 $R_{in, cm}$
 $R_{in, dm}$

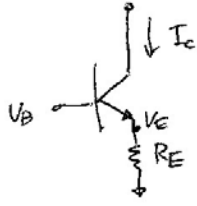
↘ half circuit (CM)



$$R_{in, cm} = \infty$$

$$A_{cm} = 0$$

3.



$$\frac{dI_C}{dV_B} (= G_m) \equiv \frac{I_C}{V_{T, \text{eff}}} \dots \textcircled{1}, \quad \frac{dI_C}{dV_{BE}} (= g_m) = \frac{I_C}{V_T} \dots \textcircled{2}$$

$$\frac{\textcircled{2}}{\textcircled{1}} \Rightarrow \frac{dV_B}{dV_{BE}} = \frac{V_{T, \text{eff}}}{V_T} \dots \textcircled{3}$$

$$V_B \equiv V_{BE} + I_C R_E \Rightarrow \frac{dV_B}{dV_{BE}} = 1 + \frac{dI_C}{dV_{BE}} \cdot R_E \dots \textcircled{4}$$

from $\textcircled{3}$, $\textcircled{4}$

$$V_{T, \text{eff}} = V_T \left(1 + \frac{dI_C}{dV_{BE}} R_E \right) = V_T (1 + g_m R_E)$$