

The Sliding-Window Lempel-Ziv Algorithm is Asymptotically Optimal

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Invited Paper

The sliding-window version of the Lempel-Ziv data-compression algorithm (sometimes called LZ '77) has been thrust into prominence recently. A version of this algorithm is used in the highly successful "Stacker" program for personal computers. It is also incorporated into Microsoft's new MS-DOS-6. Although other versions of the Lempel-Ziv algorithm are known to be optimal in the sense that they compress a data source to its entropy, optimality in this sense has never been demonstrated for this version.

In this self-contained paper, we will describe the algorithm, and show that as the "window size," a quantity which is related to the memory and complexity of the procedure, goes to infinity, the compression rate approaches the source entropy. The proof is surprisingly general, applying to all finite-alphabet stationary ergodic sources.

I. INTRODUCTION

The sliding-window version of the Lempel-Ziv (LZ) data compression algorithm (first proposed in [6] in 1977 and sometimes called LZ '77) has been thrust into prominence recently. A version of this algorithm is used in the highly successful "Stacker" program for personal computers [3]. It is also incorporated into Microsoft's new MS-DOS-6. Although other versions of the LZ algorithm are known to be optimal in the sense that they compress a data source to its entropy, such optimality has never been demonstrated for the sliding-window version.

This self-contained paper begins with a description of the sliding-window LZ algorithm. The main result is a theorem which asserts that as the "window size" (a quantity directly related to the memory and complexity requirements of the procedure) becomes large, the compression rate approaches the source entropy. This theorem is surprisingly general, applying to all stationary, ergodic, finite-alphabet sources.

We will be concerned with a data source which is a random sequence $\{X_k\}_{k=-\infty}^{\infty}$, that is stationary, ergodic,

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and takes values in the alphabet \mathcal{A} with cardinality $|\mathcal{A}| = A < \infty$. For $-\infty \leq i < j \leq \infty$, let X_i^j denote the substring $(X_i, X_{i+1}, \dots, X_j)$. Let

$$H_n = \frac{1}{n} H(X_1^n) \\ \triangleq -\frac{1}{n} \sum_{X \in \mathcal{A}^n} \Pr\{X_1^n = X\} \log(\Pr\{X_1^n = X\})$$

be the n th order (normalized) entropy of $\{X_k\}$, and let $H = \lim_{n \rightarrow \infty} H_n$ be the source entropy. (All logarithms in this paper are taken to the base 2.) It is well known that this limit always exists, and that the data source can be losslessly encoded using $(H + \epsilon)$ bits per source symbol [1], [2] (for arbitrarily $\epsilon > 0$). The LZ algorithm is a universal procedure (which does not depend on the source statistics) for encoding the source.

In Section II we give a precise description of the sliding-window LZ algorithm and state the main result. In Section III we establish the mathematical facts that we need in the proof of this theorem which we give in Section IV.

Let us remark at this point that the sliding-window LZ algorithm discussed here is not the same as the "LZ '78" algorithm, used for example in the UNIX "compress" command and in a CCITT standard for data compression for modems. In LZ '78, the "dictionary" is allowed to grow until it reaches a certain specified size. In the sliding-window version, the dictionary is of fixed size, and consists of the data symbols immediately preceding the data being compressed.

Finally, we remark that the treatment in [6], where the sliding-window LZ algorithm is first described, is nonprobabilistic. In that reference, the algorithm is shown to be optimal for a certain (deterministic) family of sources. Furthermore, for a given source in this family, the rate of convergence is similar to that of the best nonuniversal compression scheme. In the present paper, we replace the assumption that the source belongs to this family, by the more conventional (and realistic) assumption that the source is stationary and ergodic.

II. DESCRIPTION OF THE ALGORITHM

Let $\{X_k\}_{k=-\infty}^{\infty}$ be a stationary ergodic random process with entropy H , as discussed in Section I. We will now describe the sliding-window Lempel-Ziv algorithm for encoding the sequence $\{X_k\}_{k=1}^N$, where N is a large integer. Later we shall let $N \rightarrow \infty$.

Let $n_w > 0$ be an integer parameter, called the *window size*. Assume that n_w is a power of two. The first n_w symbols of X_1^N are encoded with no attempt at compression. We call $X_1^{n_w}$ the *window*. The number of bits required to encode the window $X_1^{n_w}$ is $\lceil n_w \log A \rceil$. These bits are to be considered as overhead that will be amortized over a very long time. We next define the first *phrase* $Y_1 \triangleq X_{n_w+1}^{n_w+L_1}$, where L_1 is the largest integer such that

$$X_{n_w+1}^{n_w+L_1} = X_{n_w-m}^{n_w-m+L_1-1}, \quad \text{for some } m \in [0, n_w - 1]. \quad (1)$$

Thus L_1 is the largest integer such that a copy of $X_{n_w+1}^{n_w+L_1}$ begins in the window. Let m_1 be the (say) smallest of those m 's which satisfy (1). If (1) is not satisfied for any $m \in [0, n_w-1]$, that is, $X_{n_w+1} \neq X_m$, for all $m \in [1, n_w]$, then we take $L_1 = 1$. For example if $n_w = 5$, and $(X_1, X_2, \dots) = (abcde:deda \dots)$, then $L_1 = 3$ since the string (ded) begins at position 4 ($\leq n_w$), i.e., $X_{n_w+3}^{n_w+3} = X_{n_w-1+2}^{n_w-1+2}$. Also $m_1 = 1$. Note that there is no upper bound on L_1 and in particular it can exceed n_w —for example, if $n_w = 5$ and $(X_1, X_2, \dots) = (bbbbb:aaaaaaab \dots)$, then $L_1 = 10$.

We now show how to encode the data sequence Y_1 . The first part of the encoding is the comma-free binary encoding of L_1 . One such encoding is the mapping $e(L)$ given in the Appendix. Immediately following $e(L_1)$ is a binary string s_1 , where

$$s_1 = \begin{cases} \text{binary encoding of } m_1, & \text{if } \log n_w < \lceil L_1 \log A \rceil \\ \text{binary encoding (no compression) of } Y_1, & \text{if } \log n_w \geq \lceil L_1 \log A \rceil. \end{cases} \quad (2)$$

Assume that $n_w \geq A$, so that when $L_1 = 1$, s_1 is an encoding of Y_1 . Thus the total number of bits needed to encode the first phrase $Y_1 = X_{n_w+1}^{n_w+L_1}$ is $|e(L_1)| + |s_1|$. Since $m_1 \in [0, n_w - 1]$, its binary encoding requires $\log n_w$ bits. Also $\lceil L_1 \log A \rceil$ bits are required to encode Y_1 with no compression. Thus the length of the encoding of Y_1 is

$$\begin{aligned} & |e(L_1)| + \min(\log n_w, \lceil L_1 \log A \rceil) \\ & \leq \min(\log n_w + \gamma_1 \log(L_1 + 1), \gamma_2 L_1) \end{aligned} \quad (3)$$

for suitably large γ_1, γ_2 . We made use of (A.4b) in (3).

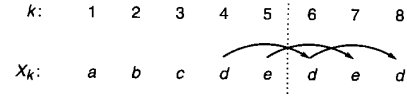
Now observe that with knowledge of the window $X_1^{n_w}$, $e(L_1)$, and s_1 , the decoder can recover $Y_1 = X_{n_w+1}^{n_w+L_1}$. Here is how. The first step is to decode $e(L_1)$ to

recover L_1 . The decoder now computes $\lceil L_1 \log A \rceil$. If this quantity is $\leq \log n_w$, the next $\lceil L_1 \log A \rceil$ bits are a binary encoding of Y_1 . Otherwise, the next $\log n_w$ bits define a pointer to position $(n_w - m_1)$ where a copy of Y_1 begins. This position is within the window, i.e., $n_w - m_1 \in [1, n_w]$. The decoder copies $X_{n_w-m_1}$ into position $n_w + 1$, then $X_{n_w-m_1+1}$ into position $n_w + 2$, etc. When $X_{n_w-m+L_1-1}$ is copied into position $n_w + L_1$, the process is complete and Y_1 is reconstructed.

As an example, consider again the case $n_w = 5$, where

$$(X_1, X_2, \dots) = (abcde:deda \dots).$$

As above, $L_1 = 3$ and $m_1 = 1$. With knowledge of the window, $X_1^{n_w} = (abcde)$, the decoder can copy "d" and "e" to positions 6 and 7, respectively, and then copy the "d" in position 6 to position 8:



Thus $Y_1 = (ded)$.

After the first phrase Y_1 is encoded, the first L_1 symbols in the window are deleted and the L_1 symbols of Y_1 are added at the end of the window. Thus the new window is $X_{L_1+1}^{L_1+n_w}$, and has length n_w . Phrase 2 is now constructed using the new window and data $X_{n_w+L_1+1}, X_{n_w+L_1+2}, \dots$. The process is repeated until the N symbols are exhausted. The phrases are Y_1, Y_2, \dots, Y_c and their lengths are L_1, L_2, \dots, L_c , respectively. The last phrase Y_c is terminated prematurely in the obvious way when the data are exhausted.

From (3), the total number of bits to encode X_1^N is

$$\begin{aligned} \nu(X_1^N) &= \sum_{i=1}^c \{ |e(L_i)| + \min(\log n_w, \lceil L_i \log A \rceil) \} \\ &\quad + \lceil n_w \log A \rceil \end{aligned} \quad (4)$$

where the last term is overhead for the first window. Note that c and the $\{L_i\}_{i=1}^c$ are random variables. The average rate is $\bar{R}(N) \triangleq E[\nu(X_1^N)]/N$. Using the bound of (3) we have

$$\begin{aligned} \bar{R}(N) &\leq \frac{\lceil n_w \log A \rceil}{N} \\ &\quad + \frac{1}{N} E \sum_{i=1}^c \min(\log n_w + \gamma_1 \log(L_i + 1), \gamma_2 L_i) \end{aligned}$$

(5)

We are now ready to state our main result.

Theorem 2.1 $\lim_{n_w \rightarrow \infty} \lim_{N \rightarrow \infty} \bar{R}(N) = H$

It is interesting to note that the version of the sliding-window LZ algorithm used by Stac in their Stacker program

Proof: Write, for fixed $\epsilon > 0$, $\delta = \epsilon/2$, and $T_\ell(\delta)$ defined by (6)

$$\begin{aligned} & \Pr\{W_\ell > 2^{\ell(H+\epsilon)}\} \\ &= \sum_{z \in T_\ell(\delta)} \Pr\{X_0^{\ell-1} = z\} \Pr\{W_\ell > 2^{\ell(H+\epsilon)} | X_0^{\ell-1} = z\} \\ & \quad + \sum_{z \notin T_\ell(\delta)} \Pr\{X_0^{\ell-1} = z\} \Pr\{W_\ell > 2^{\ell(H+\epsilon)} | X_0^{\ell-1} = z\} \\ & \leq \sum_{z \in T_\ell(\delta)} \Pr\{X_0^{\ell-1} = z\} \frac{1}{2^{\ell(H+\epsilon)} \Pr\{X_0^{\ell-1} = z\}} \\ & \quad + \Pr\{X_0^{\ell-1} \notin T_\ell(\delta)\}. \end{aligned} \quad (14)$$

The inequality in (14) follows from (13) with $n = 2^{\ell(H+\epsilon)}$. Now for $z \in T_\ell(\delta)$, $\Pr\{X_0^{\ell-1} = z\} \geq 2^{-\ell(H+\delta)}$. Thus from (14), with $\epsilon - \delta = \epsilon/2$

$$\begin{aligned} \Pr\{W_\ell > 2^{\ell(H+\epsilon)}\} &\leq 2^{-\ell(\epsilon-\delta)} \Pr\{X_0^{\ell-1} \in T_\ell(\delta)\} \\ & \quad + \Pr\{X_0^{\ell-1} \notin T_\ell(\delta)\} \rightarrow 0, \\ & \quad \text{as } \ell \rightarrow \infty \end{aligned} \quad (15)$$

by Theorem 3.1 (AEP). This is Theorem 3.3.

We will use the following form of Theorem 3.3:
Corollary 3.4 Let $n(\ell)$, $\ell = 1, 2, \dots$, satisfy

$$L \triangleq \lim_{\ell \rightarrow \infty} \frac{1}{\ell} \log n(\ell) > H. \quad (16a)$$

Then

$$\lim_{\ell \rightarrow \infty} \Pr\{W_\ell > n(\ell)\} = 0. \quad (16b)$$

Proof: Let $\epsilon = L - H > 0$. For $\ell \geq \ell_0$ (sufficiently large), $(1/\ell) \log n(\ell) \geq L - (\epsilon/2) = H + (\epsilon/2)$. Thus

$$n(\ell) \geq 2^{\ell[H+(\epsilon/2)]}.$$

Thus for $\ell \geq \ell_0$

$$\Pr\{W_\ell > n(\ell)\} \leq \Pr\{W_\ell > 2^{\ell[H+(\epsilon/2)]}\} \rightarrow 0$$

by Theorem 3.3.

IV. PROOF OF THEOREM 2.1

That $\bar{R}(N) \geq H$ for all N follows from the converse to the Coding Theorem for lossless source coding. Since the algorithm defined in Section II yields a prefix-free ("instantaneous") code for X_1, \dots, X_N

$$E\nu(X_1^N) \geq H(X_1, \dots, X_N).$$

(See Theorem 5.3.1 in [1].) Since $H(X_1, \dots, X_N) \geq NH$, $\bar{R}(N) = E\nu(X_1^N)/N \geq H$.

We now show that $\lim \bar{R}(N) \leq H$. Suppose that we have implemented the algorithm to encode X_1, \dots, X_N . Subdivide the interval $[n_w + 1, N]$ into N'/ℓ_0 subintervals of length ℓ_0 , where

$$N' = N - n_w \quad (17a)$$

and

$$\ell_0 = \frac{\log n_w}{H + \epsilon} \quad (17b)$$

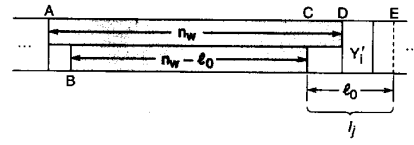


Fig. 1.

and $\epsilon > 0$ is arbitrary. (Assume that ϵ is adjusted so that ℓ_0 is an integer, and that ℓ_0 divides N'). Recall that $X_1^{n_w}$ is the (uncoded) initial window. Denote the N'/ℓ_0 subintervals by $\{I_j\}$, where

$$I_j = [n_w + (j-1)\ell_0 + 1, n_w + j\ell_0], \quad j = 1, 2, \dots, N'/\ell_0.$$

We say that a subinterval I_j is *bad* if a copy of $\{X_k\}_{k \in I_j}$ does not begin in the string of $(n_w - \ell_0)$ symbols preceding it, i.e.

$$X_{n_w+(j-1)\ell_0+1}^{n_w+j\ell_0} \neq X_{n_w+(j-1)\ell_0+1-m}^{n_w+j\ell_0-m}, \quad 1 \leq m \leq n_w - \ell_0. \quad (18)$$

Now referring to the discussion in Section III, we have that

$$\Pr\{I_j \text{ is bad}\} = \Pr\{W(\ell_0) > n_w - \ell_0\}. \quad (19)$$

Since $n(\ell_0) \triangleq n_w - \ell_0 = 2^{\ell_0(H+\epsilon)} - \ell_0$ satisfies (16a), with $L = H + \epsilon$, Corollary 3.4 implies that

$$\Pr\{I_j \text{ is bad}\} \rightarrow 0, \quad (20)$$

as n_w (and ℓ_0) $\rightarrow \infty$.

Now let $\{Y_i\}, 1 \leq i \leq c$ be the phrases generated by the algorithm when encoding X_1^N . For $1 \leq i \leq c$, let Y'_i be the phrase Y_i augmented by the next symbol from X_1^N . Thus if $Y_i = X_k^{k+L_i-1}$, then $Y'_i = X_k^{k+L_i}$. We say that the phrase Y_i is in *internal* phrase, if the corresponding augmented phrase Y'_i begins and ends in the same subinterval I_j . We claim that if Y_i is an internal phrase supported on I_j , then I_j is a bad subinterval. We show this with the aid of the schematic diagram in Fig. 1. The figure shows the augmented internal phrase Y'_i supported on the interval I_j . The window corresponding to phrase Y_i is supported on the interval AD . By definition, a copy of Y'_i does *not* begin in this window (since Y_i is the *longest* sequence, beginning at D , a copy of which begins in window). Since Y'_i is supported on I_j , a copy of $\{X_k\}_{k \in I_j}$ cannot begin in the window AC , and therefore cannot begin in BC (since B is to the right of A). Thus I_j is a bad subinterval.

Let $S_I = \{i : Y_i \text{ is internal}\}$, and let ψ be the fraction of the intervals $\{I_j\}$ which are bad. It follows that

$$\begin{aligned} \sum_{i \in S_I} |Y_i| &\leq \ell_0 \{\text{no. of bad intervals}\} \\ &\leq \ell_0 \frac{N'}{\ell_0} \psi = N' \psi. \end{aligned} \quad (21)$$

We are now ready to complete the proof to Theorem 2.1. Rewrite inequality (5) as

$$\bar{R}(N) \leq \frac{\lceil n_w \log A \rceil}{N} + \frac{1}{N} E \left\{ \sum_{i \in S_I} \gamma_2 L_i + \sum_{i \in S_I^c} [\log n_w + \gamma_1 \log(L_i + 1)] \right\} \quad (22)$$

Now the first expectation is from (21)

$$\frac{1}{N} E \sum_{i \in S_I} \gamma_2 L_i \leq \frac{\gamma_2 N'}{N} E \psi \leq \gamma_2 \Pr \{I_j \text{ is bad}\}. \quad (23)$$

Finally, observe that if Y_i is *not* an internal phrase, then Y_i must occupy the last position of some subinterval I_j . Thus

$$c' \triangleq |S_I^c| \leq \{\text{number of subintervals}\} = \frac{N'}{\ell_0}. \quad (24)$$

The second term in (22) (without the expectation) is

$$\begin{aligned} & \frac{1}{N} \sum_{i \in S_I^c} \log n_w + \gamma_1 \frac{1}{N} \sum_{i \in S_I^c} \log(L_i + 1) \\ &= |S_I^c| \frac{\log n_w}{N} + \gamma_1 \frac{c'}{N} \sum_{i \in S_I^c} \log(L_i + 1) \\ &\stackrel{(a)}{\leq} |S_I^c| \frac{\log n_w}{N} + \gamma_1 \frac{c'}{N} \log \left(\frac{1}{c'} \sum L_i + 1 \right) \\ &\stackrel{(b)}{\leq} \frac{N'}{N} \frac{\log n_w}{\ell_0} + \gamma_1 \frac{c'}{N} \log \left(\frac{N}{c'} + 1 \right) \\ &\stackrel{(c)}{\leq} \frac{\log n_w}{\ell_0} + \frac{\gamma_1}{\ell_0} \log(\ell_0 + 1) \\ &\stackrel{(d)}{=} (H + \epsilon) + (\gamma_1/\ell_0) \log(\ell_0 + 1). \end{aligned} \quad (25)$$

Step (a) in (25) follows from the concavity of $\log(\cdot)$; step (b) from $\sum_{i \in S_I^c} L_i \leq N$; step (c) from the fact that $(1/x) \log(x+1)$, $x \geq 0$, is decreasing in x , and from (24) which implies

$$\frac{c'}{N} \leq \frac{N'}{N\ell_0} \leq \frac{1}{\ell_0}$$

and step (d) from (17b).

Substituting (23) and (25) into (22) we have

$$\bar{R}(N) \leq \frac{\lceil n_w \log A \rceil}{N} + \gamma_2 \Pr \{I_j \text{ bad}\} + H + \epsilon + (\gamma_1/\ell_0) \log(\ell_0 + 1)$$

and

$$\lim_{N \rightarrow \infty} \bar{R}(N) \leq \gamma_2 \Pr \{I_j \text{ is bad}\} + H + \epsilon + (\gamma_1/\ell_0) \log(\ell_0 + 1).$$

Finally, letting $n_w \rightarrow \infty$, and using (20) we have

$$\lim_{n_w \rightarrow \infty} \lim_{N \rightarrow \infty} \bar{R}(N) \leq H + \epsilon$$

which is Theorem 2.1, on letting $\epsilon \rightarrow 0$.

APPENDIX

COMMA-FREE CODING OF AN UNBOUNDED INTEGER

In this Appendix we define a scheme for unambiguously encoding an integer L into a binary string. Let $\{0, 1\}^*$ be the set of binary sequences of arbitrary length. We will give an encoding or mapping $e: [1, \infty) \rightarrow \{0, 1\}^*$, which maps the nonnegative integers into binary sequences, such that for any distinct L_1, L_2 , $e(L_1)$ is not a prefix of $e(L_2)$. Thus the code is uniquely decipherable, see for example [1, ch. 5].

For $k \in [1, \infty)$ let $b(k)$ be the binary expansion of the integer k . Thus $b(1) = 1, b(2) = 10$, etc. The length of this expansion is

$$|b(k)| = \lceil \log(k+1) \rceil. \quad (A1)$$

Also, for $k = 1, 2, \dots$, let $u(k) \triangleq 0^{k-1}1$, the concatenation of $(k-1)$ 0's followed by a 1. First observe that

$$\hat{e}(k) = u(|b(k)|) * b(k) \quad (A2)$$

where $*$ denotes concatenation, is a prefix-free encoding of $k \in [1, \infty)$. For example, if $\hat{e}(k_1) = 00011001$, the prefix 0001 tells us that the next 4 bits, 1001, are the binary encoding of $k_1 = 9$.

The mapping which we will use is, for $L = 1, 2, \dots$

$$e(L) = \hat{e}(|b(L)|) * b(L). \quad (A3)$$

The prefix $\hat{e}(|b(L)|)$ encodes the length of $b(L)$, and the next $|b(L)|$ bits is the binary expansion of L . For example, when $L = 7, b(L) = 111$, and $|b(L)| = 3$ so that $\hat{e}(|b(L)|) = 0111$. Thus $e(L) = e(7) = 0111111$.

We need a bound on $|e(L)|$. From (A2) $|\hat{e}(k)| = 2|b(k)|$. Thus from (A3),

$$|e(L)| = 2|b(|b(L)|)| + |b(L)|.$$

Using (A1) we see that for large L ,

$$|e(L)| \sim \log L + 2 \log \log L.$$

We can account for small values of L by writing, for *all* $L = 1, 2, \dots$,

$$|e(L)| \leq \log(L+1) + \gamma \log \log(L+2) \quad (A4a)$$

for a suitably large γ . For our purposes the very weak bound

$$|e(L)| \leq \gamma \log(L+1) \quad (A4b)$$

will suffice, where γ is appropriately large, say $\gamma = 10$.

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